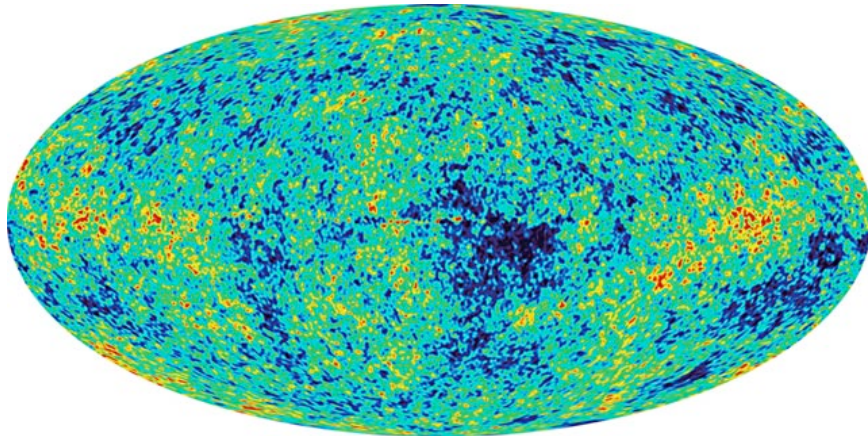


Structures et leur évolution

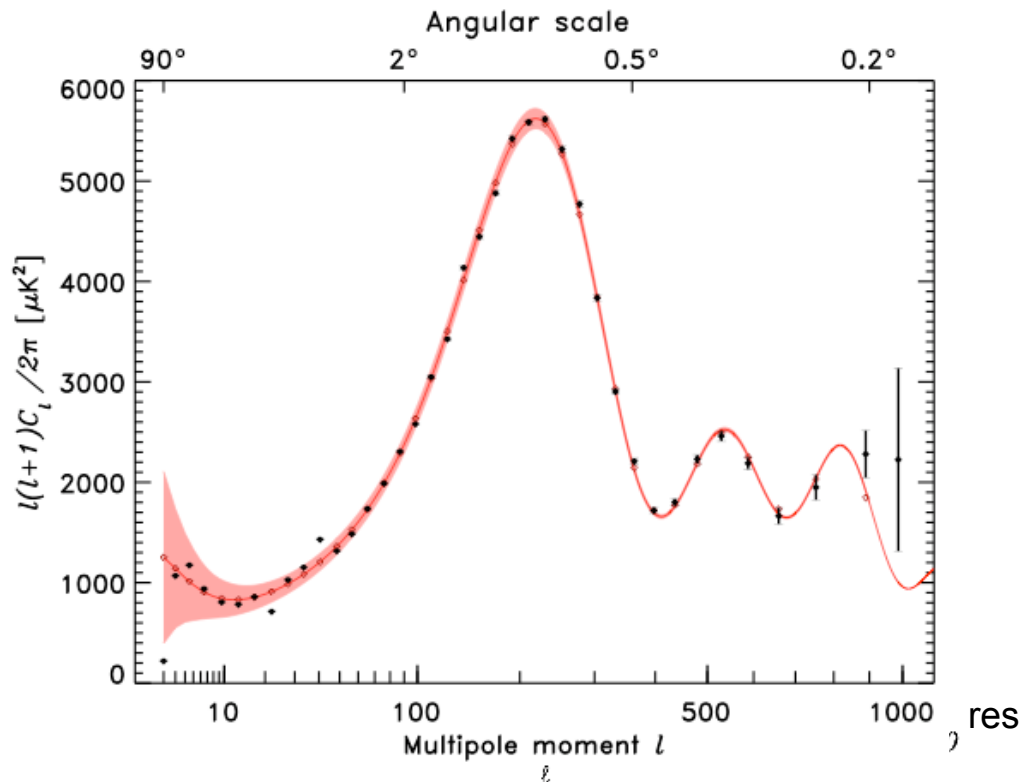
Cours 7 : Le fond cosmologique (CMB)

The Temperature Anisotropies



$$\Delta_T(\hat{n}) = \sum a_{lm} Y_{lm}(\hat{n})$$

Random variables



$$\langle a_{lm} \rangle = 0$$

$$\langle a_{lm} a_{l'm'}^* \rangle = C_l \delta_{ll'} \delta_{mm'}$$

Statistical isotropy

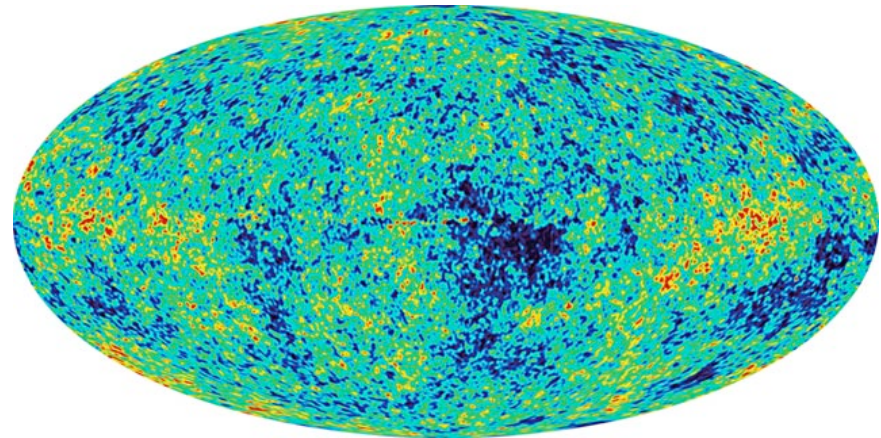
Angular power spectrum

Cosmic Variance

Given an all-sky map, we define the power spectrum estimator as:

$$\hat{C}_l = \frac{1}{2l+1} \sum_{m=-l}^l |a_{lm}|^2$$

We have $2l+1$ independent measurements to estimate the variance C_l at given l



■ Unbiased estimator:

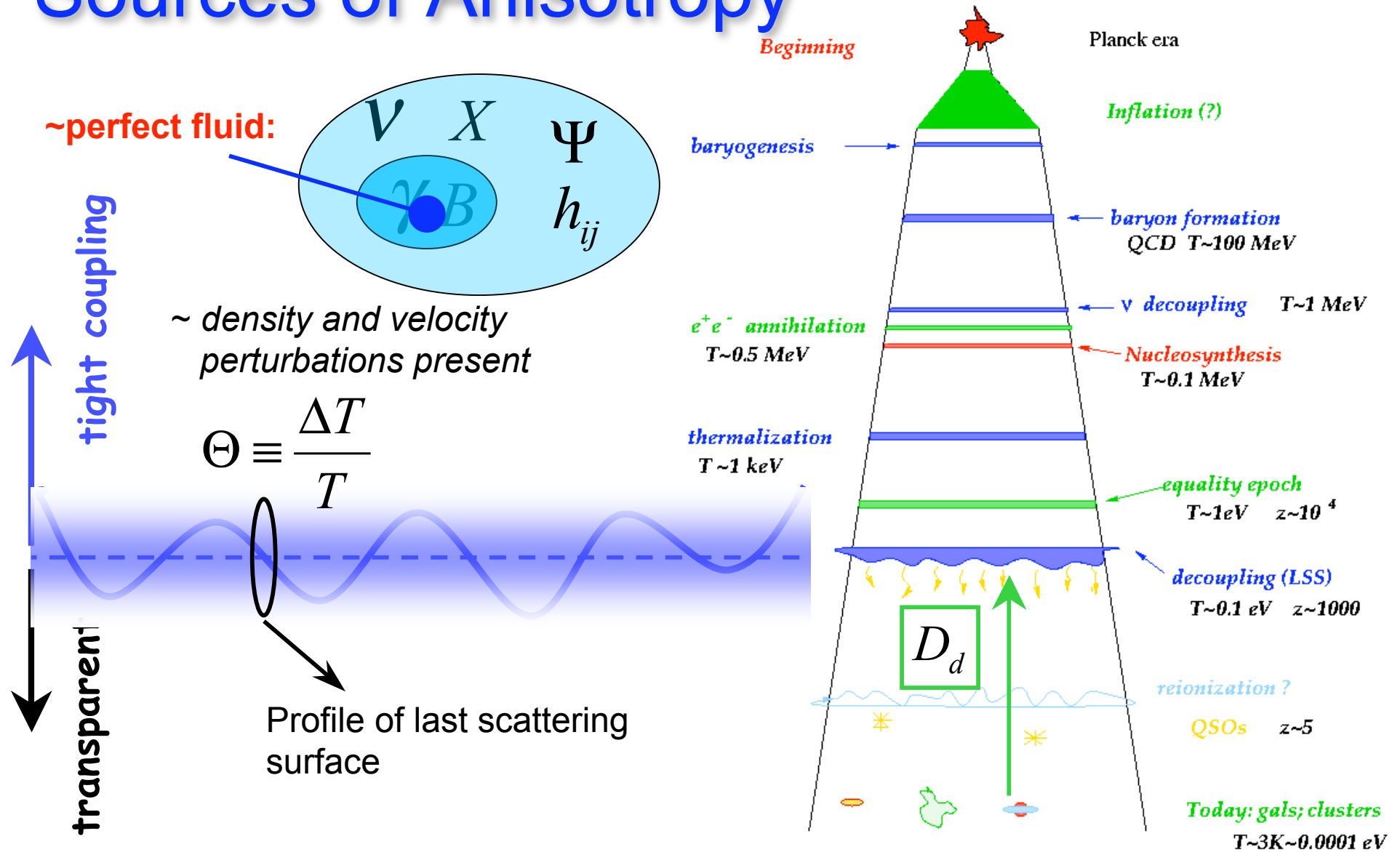
$$\langle \hat{C}_l \rangle = C_l$$

■ Variance of estimator:

$$\text{Var}(\hat{C}_l) = \frac{2}{2l+1} C_l^2$$

Cosmic Variance
Intrinsic: one sky

Sources of Anisotropy



Baryon-photon fluid

$$\left. \begin{aligned} \rho &= \rho_B + \rho_\gamma \\ p &= p_B + p_\gamma \approx \frac{1}{3} \rho_\gamma \end{aligned} \right\} \text{Photon/pressure dominated}$$

$$\Theta \equiv \frac{\Delta T}{T} = \frac{1}{4} \frac{\Delta \rho_\gamma}{\rho}$$

$$\Theta(k, \tau) \approx A \cos(ks + \delta)$$

$$s = \int_0^\tau d\eta c_s$$

Oscillations
(sound waves)

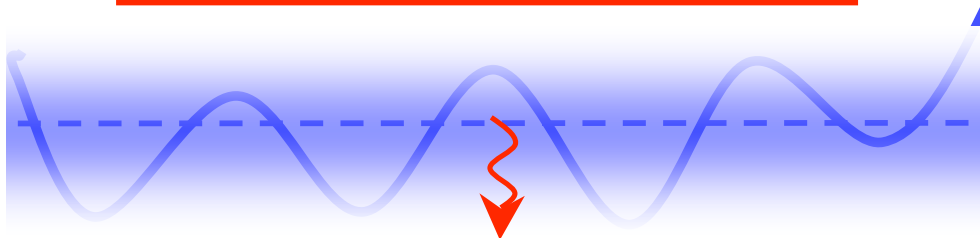
adiabatic

$$c_s^2 = \delta p / \delta \rho$$

Initial conditions

$$\begin{aligned} \Theta(k, 0) &= -\frac{2}{3} \Psi \\ \dot{\Theta}(k, 0) &= 0 \end{aligned}$$

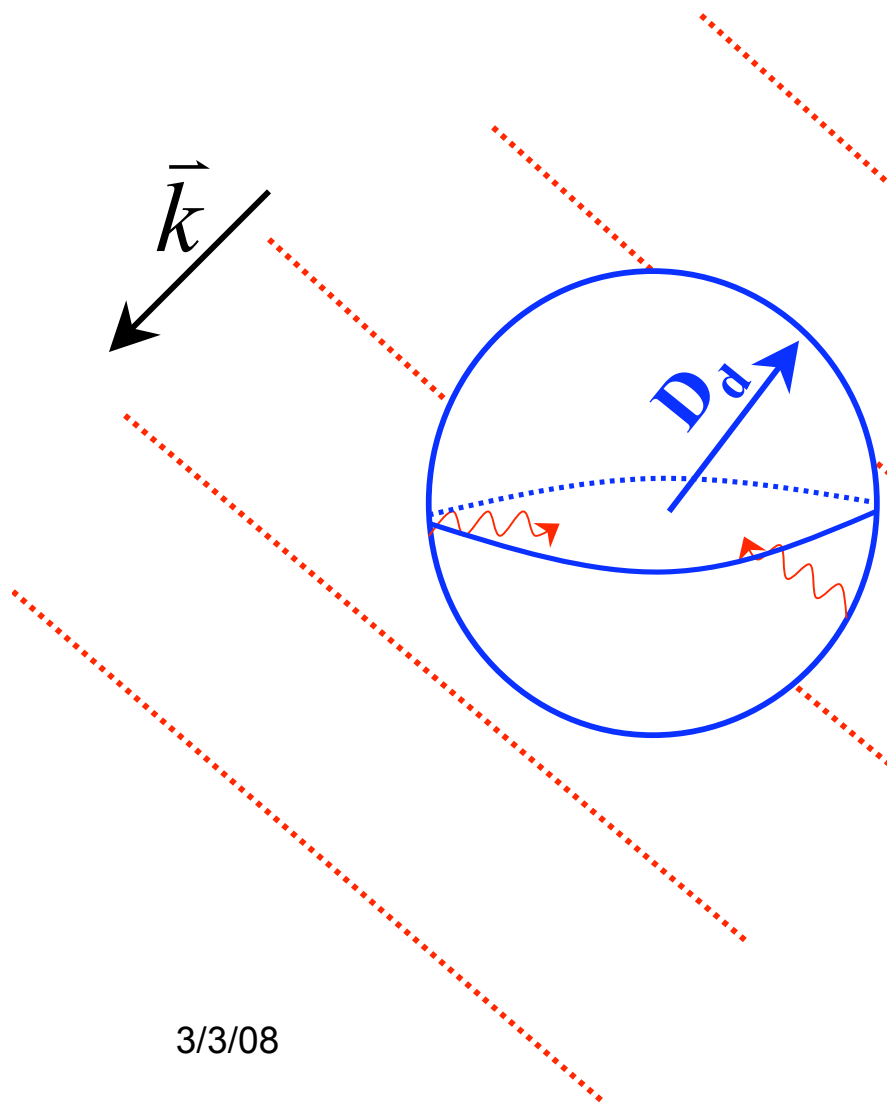
Curvature perturbations
(scalar metric perts)



$$\Theta + \Psi$$

Over-dense/hot region
→ Gravitational redshift

Projection onto the Sky



$$\Delta_T(\hat{n}) = \frac{1}{(2\pi)^3} \int d^3k [\Theta + \Psi](k, \tau_d) e^{-i\vec{k} \cdot D_d \hat{n}}$$

$$= \sum_{lm} a_{lm} Y_{lm}(\hat{n})$$

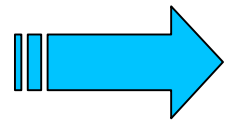
$$e^{-i\vec{k} \cdot \vec{x}} = 4\pi \sum_{lm} (-i)^l j_l(kx) Y_{lm}^*(\hat{k}) Y_{lm}(\hat{x})$$

$$a_{lm} = \frac{i^l}{2\pi^2} \int d^3k [\Theta + \Psi] j_l(kD_d) Y_{lm}^*(\hat{k})$$

$$C_l = 4\pi \int \frac{dk}{2\pi^2} \underbrace{j_l^2(kD_d)} k^2 P_\Theta(k)$$

Peak: $l \sim kD_d$

$$(\Psi \approx \text{const})$$



$$\Theta(k, \tau) + \Psi(k, 0) = \Psi(k, 0) \left(1 - \frac{2}{3} \cos(ks) \right)$$

$$v = \frac{1}{\sqrt{3}} \Psi(k, 0) \sin(ks)$$

Coherent

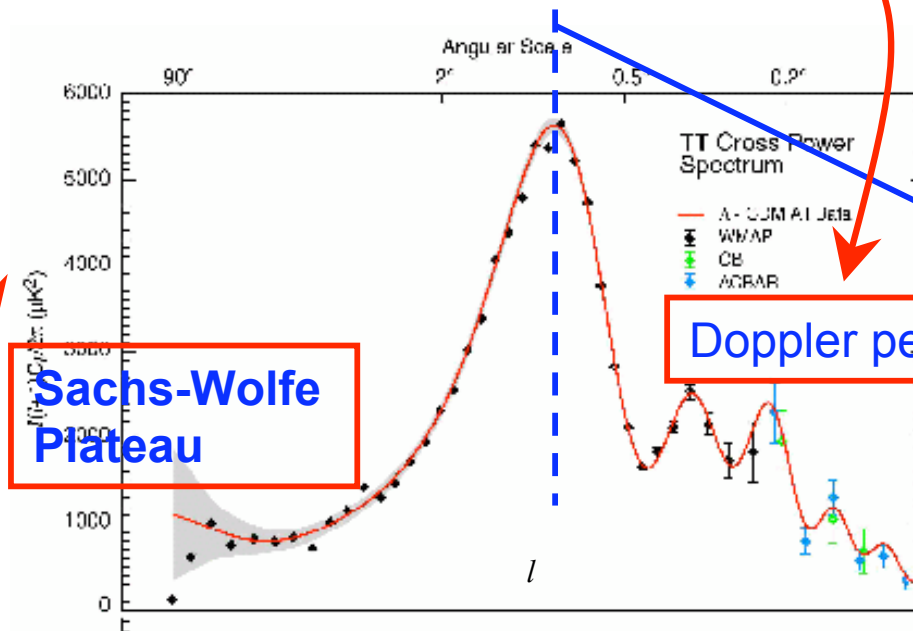
$$\delta = 0 \quad \forall k$$

$$\Theta(k, \tau_d) + \Psi \xrightarrow{ks_d \ll 1} \frac{1}{3} \Psi(k, 0)$$

Large scales: initial conditions

$$\Theta(k, \tau_d) + \Psi \xrightarrow{ks_d \gg 1} \text{oscillations}$$

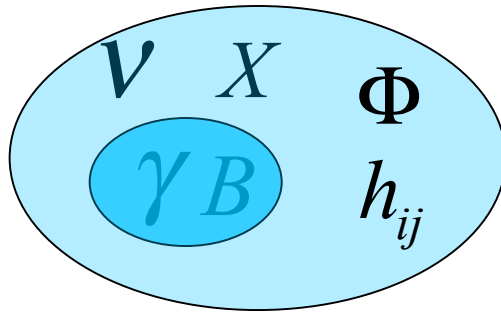
Small scales: sound waves



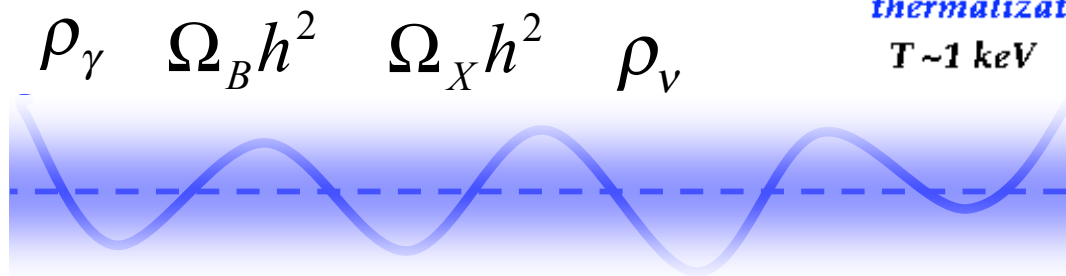
$$s_d = \int_0^{\eta_d} d\eta c_s$$

(Sound) Horizon at decoupling

$$l_d \sim \frac{D_d(H_0, \Omega, \Lambda)}{s_d}$$



Relative heights
= fluid composition

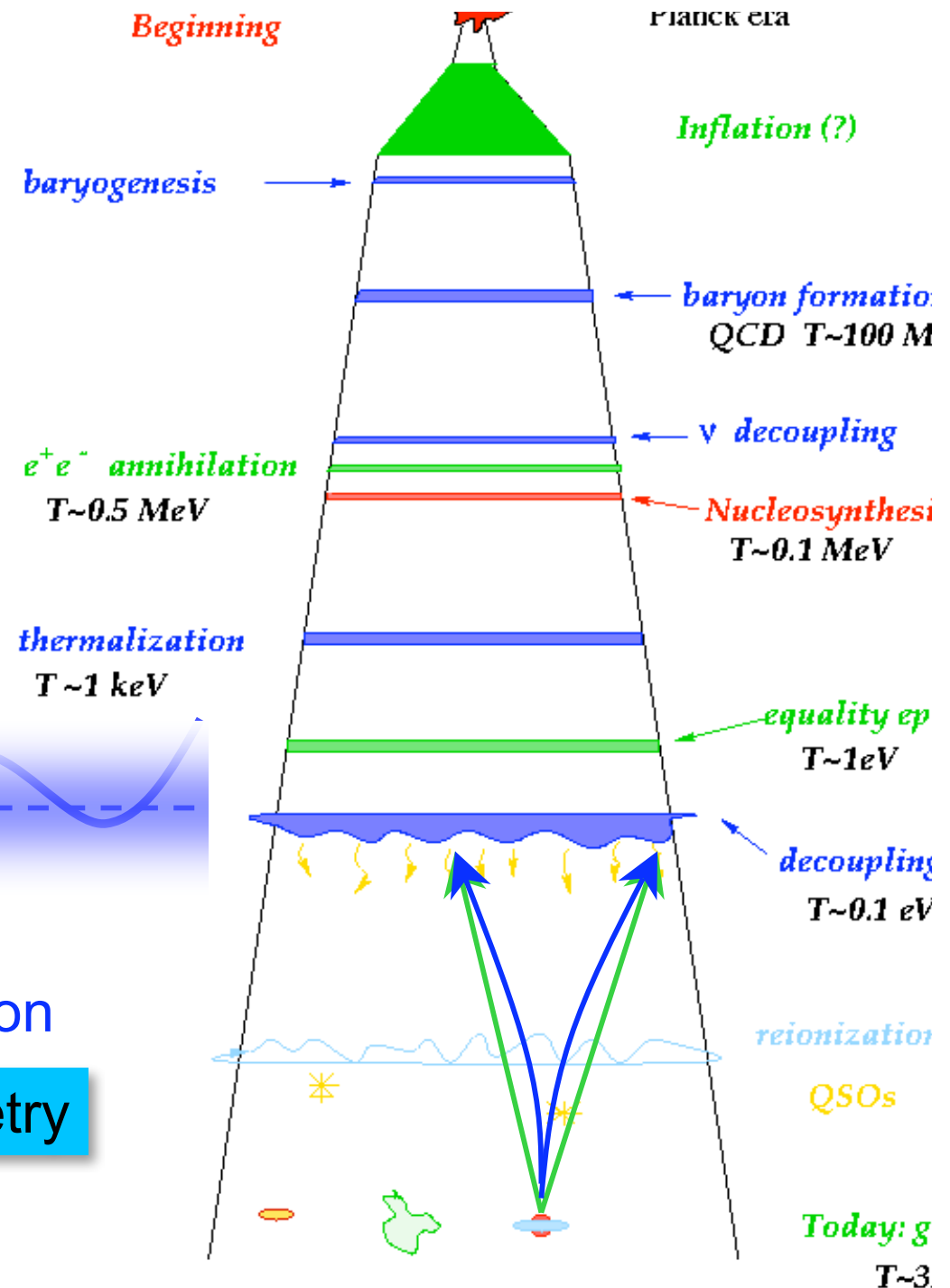


Flat space projection

Curved space projection

Peak position ~ Geometry

3/3/08



Peak position/separation

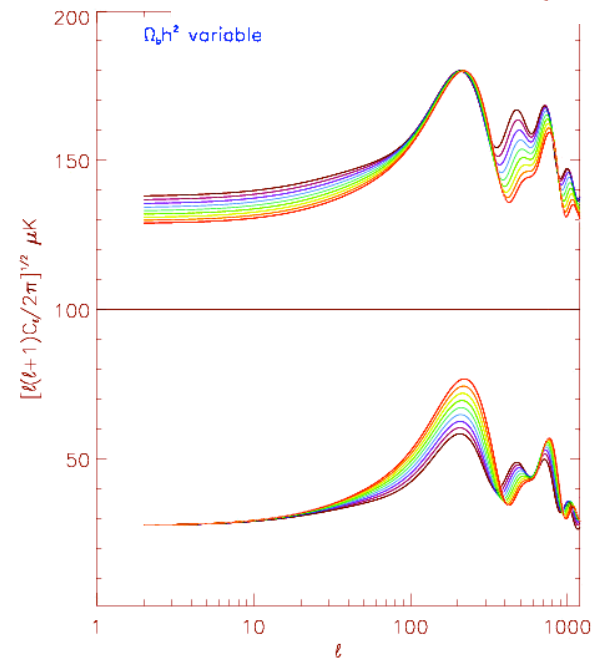
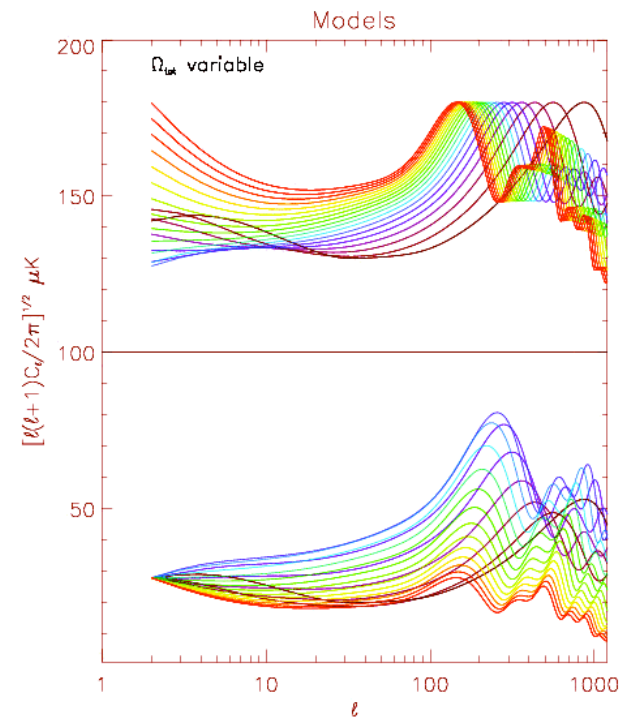
geometry

Peak heights

densities

$$h^2 = \frac{\Omega_B h^2 + \Omega_X h^2}{1 - \Omega_\Lambda - \Omega_R}$$

3/3/08



(M. Douspis/
M. Le Dour)

CMBFast

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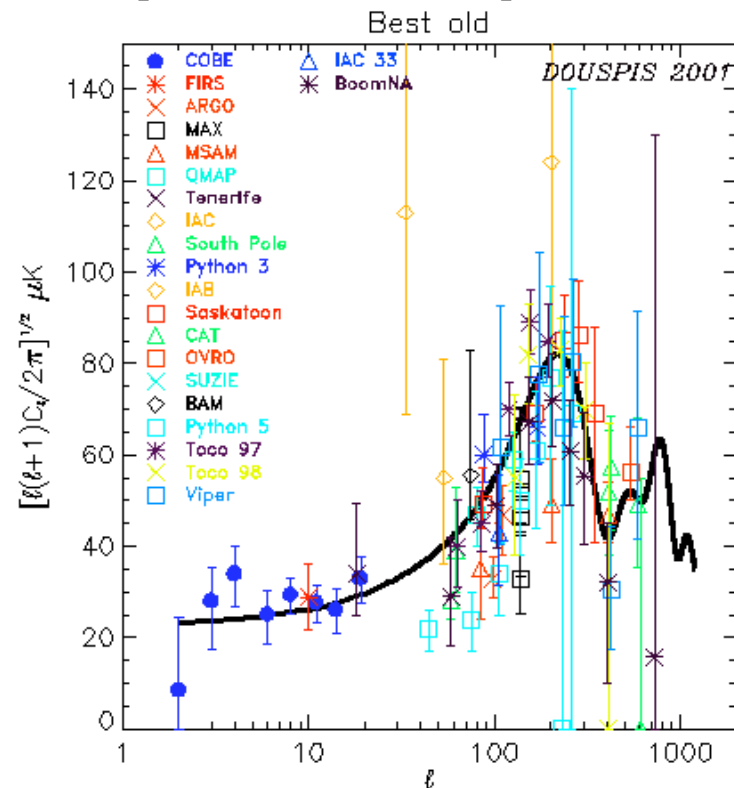
Some Results

★ CMB anisotropies: 3 generations...

First generation

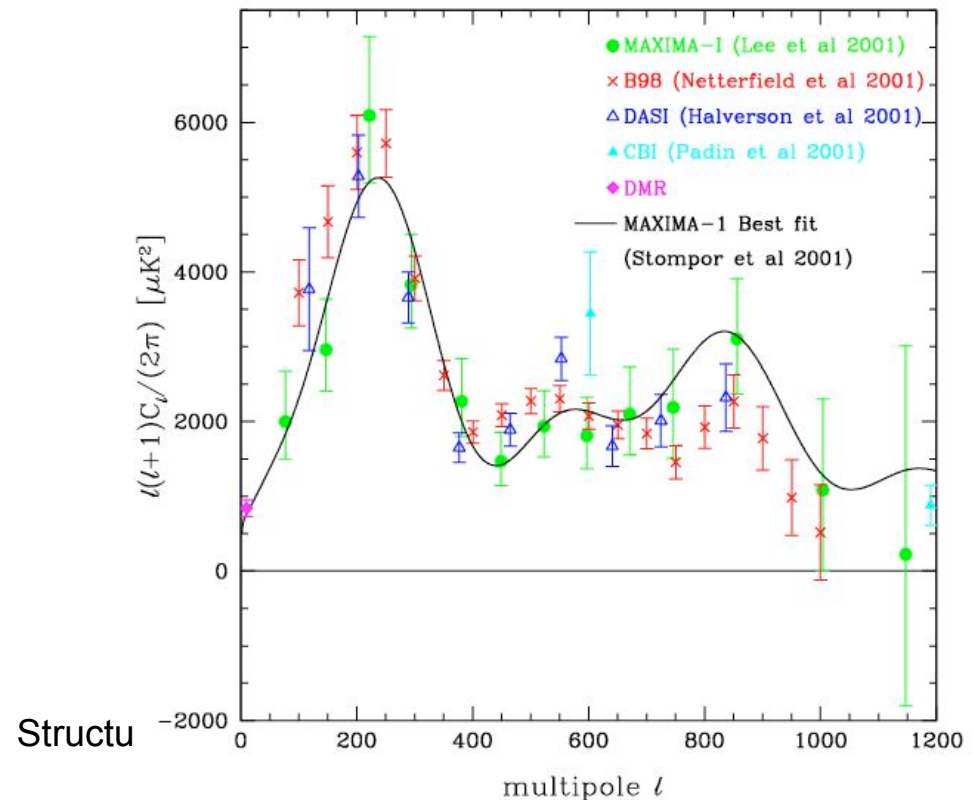
Douspis et al.

<http://webast.ast.obs-mip.fr/cosmo/CMB>

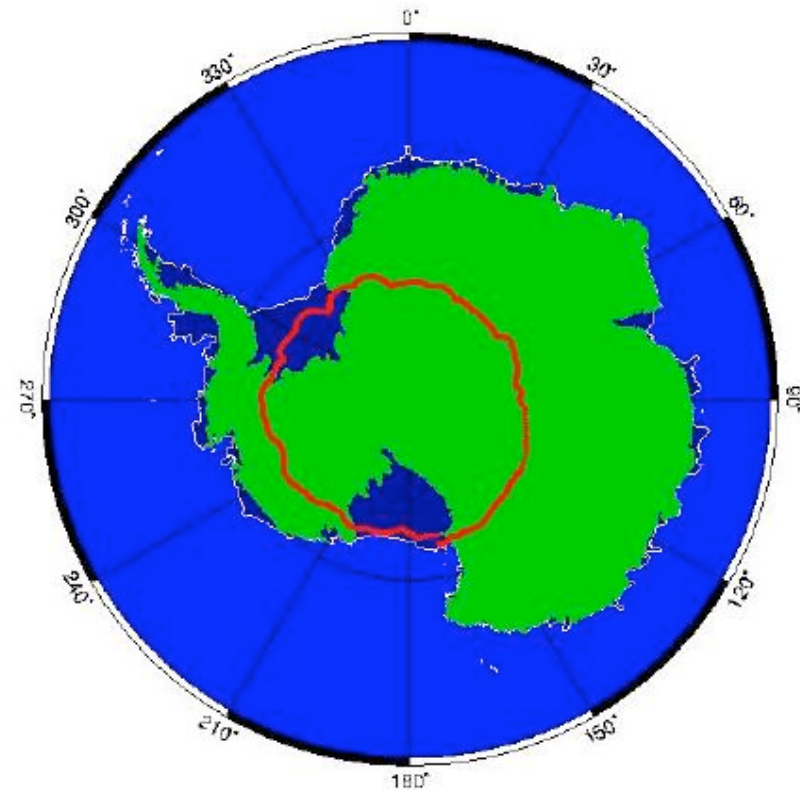


BOOMERanG/MAXIMA/ DASI

MAXIMA team (<http://aether.lbl.gov/>)



BOOMERanG: (29 Dec 1998 - 9 Jan 1999)

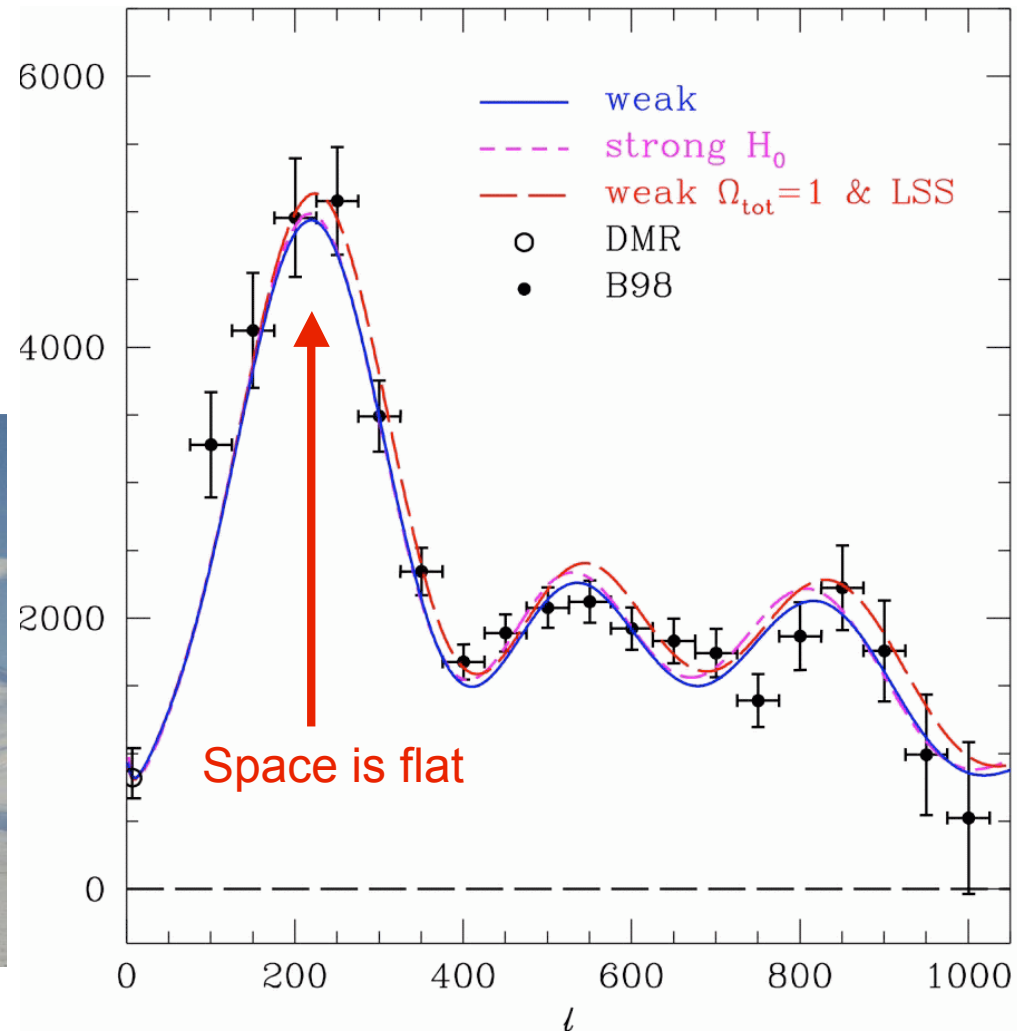


BOOMERanG (Results 2000)

South Pole flight



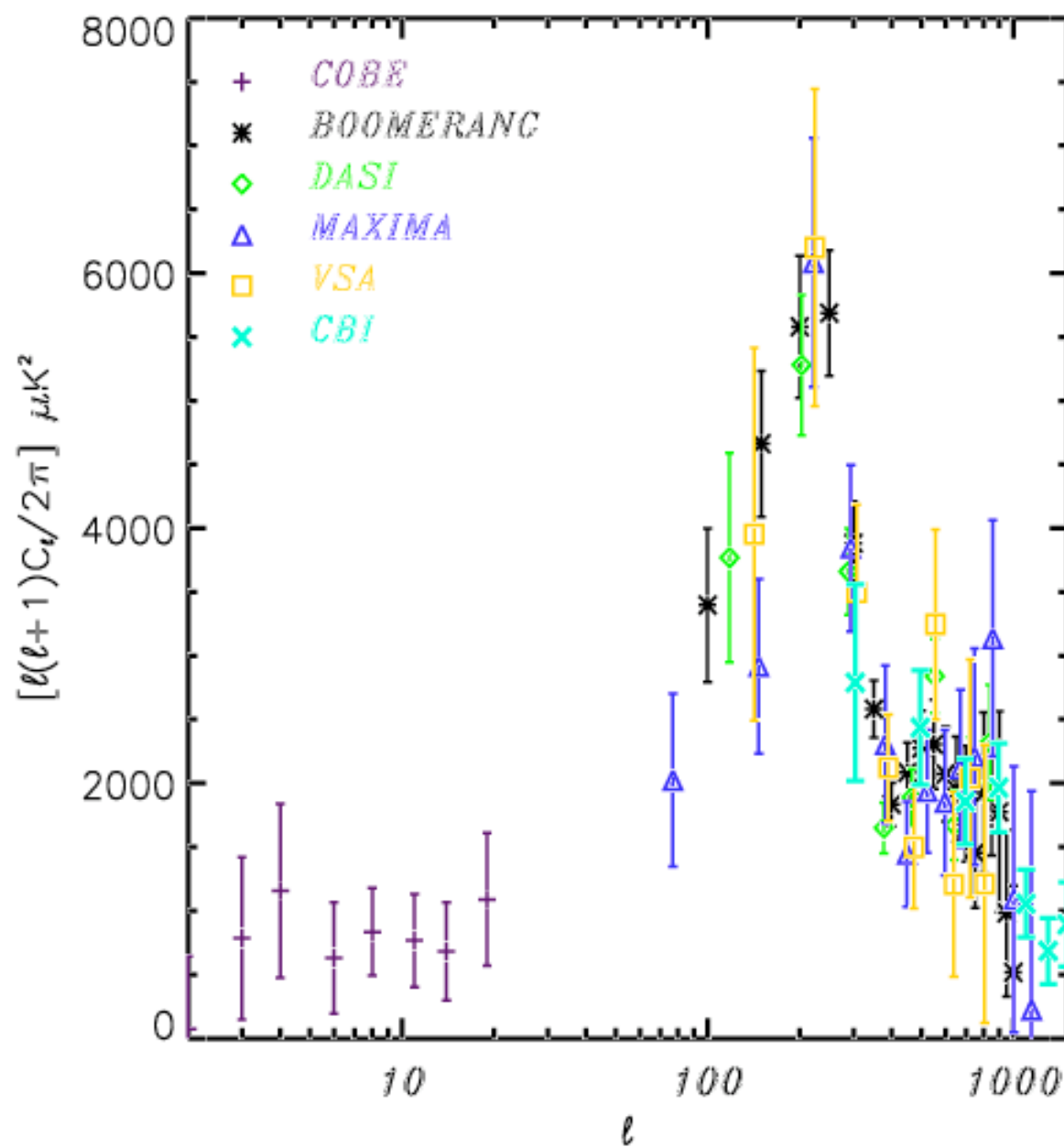
3/3/08



Structures

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Before Archeops



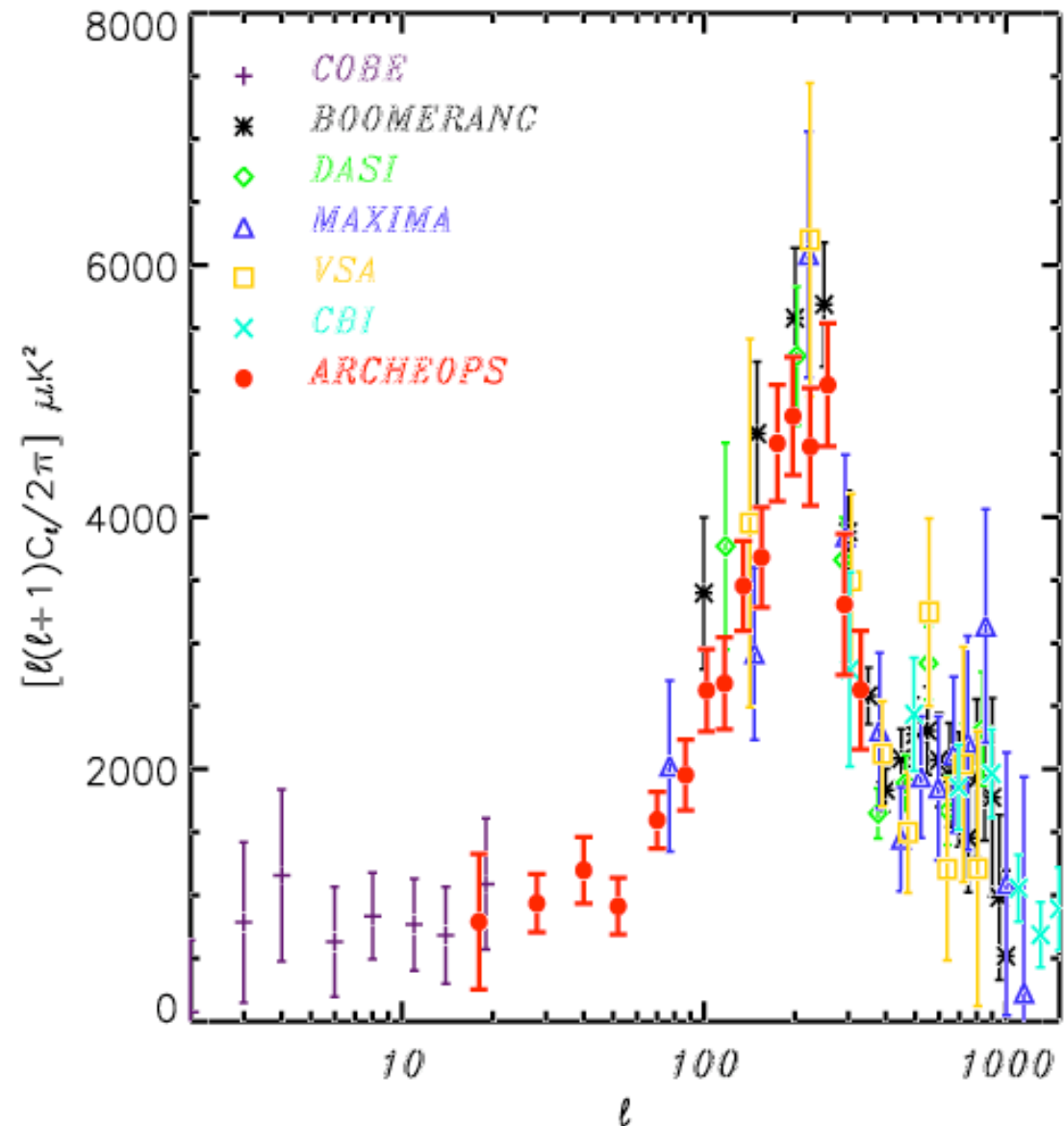
Archeops

Une seule expérience
couvre des échelles
de COBE au premier
pic acoustique



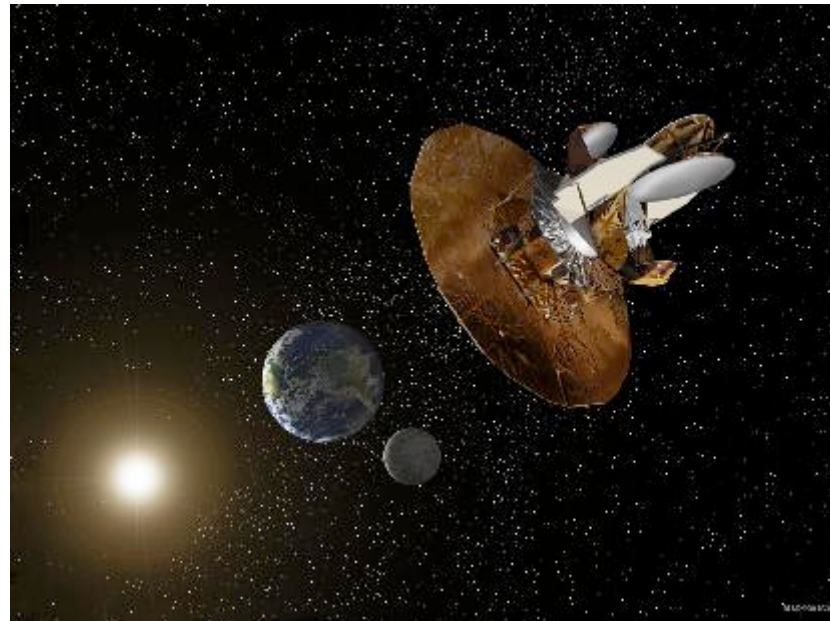
5/5/06

Benoît et al. 2003



Wilkinson Microwave Anisotropy Probe (WMAP)

- Launch: June 30, 2001
- Orbit at L2
- All-sky observations
- First-year data release: 2/2003
- Three-year data release: 3/2006
 - Polarization data
- Five-year data release: 3/2008



Space is Flat

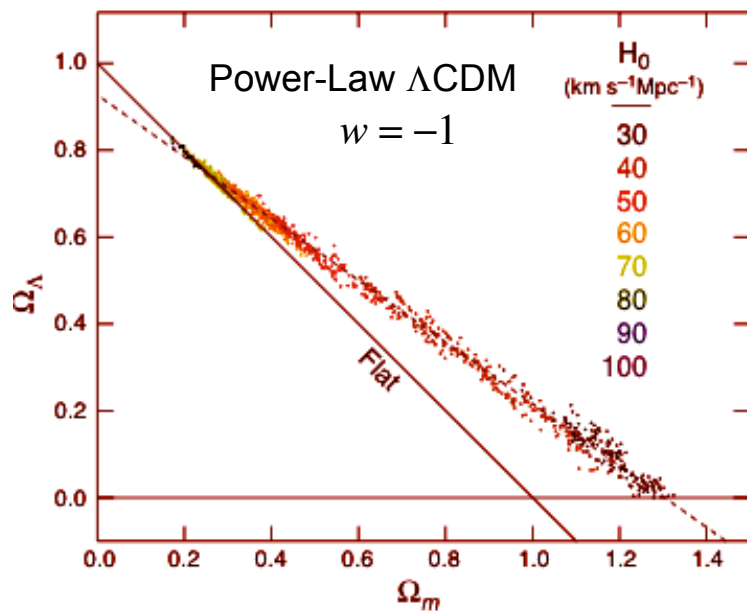
WMAP 3

+ HST: $h = 0.72 \pm 0.08$

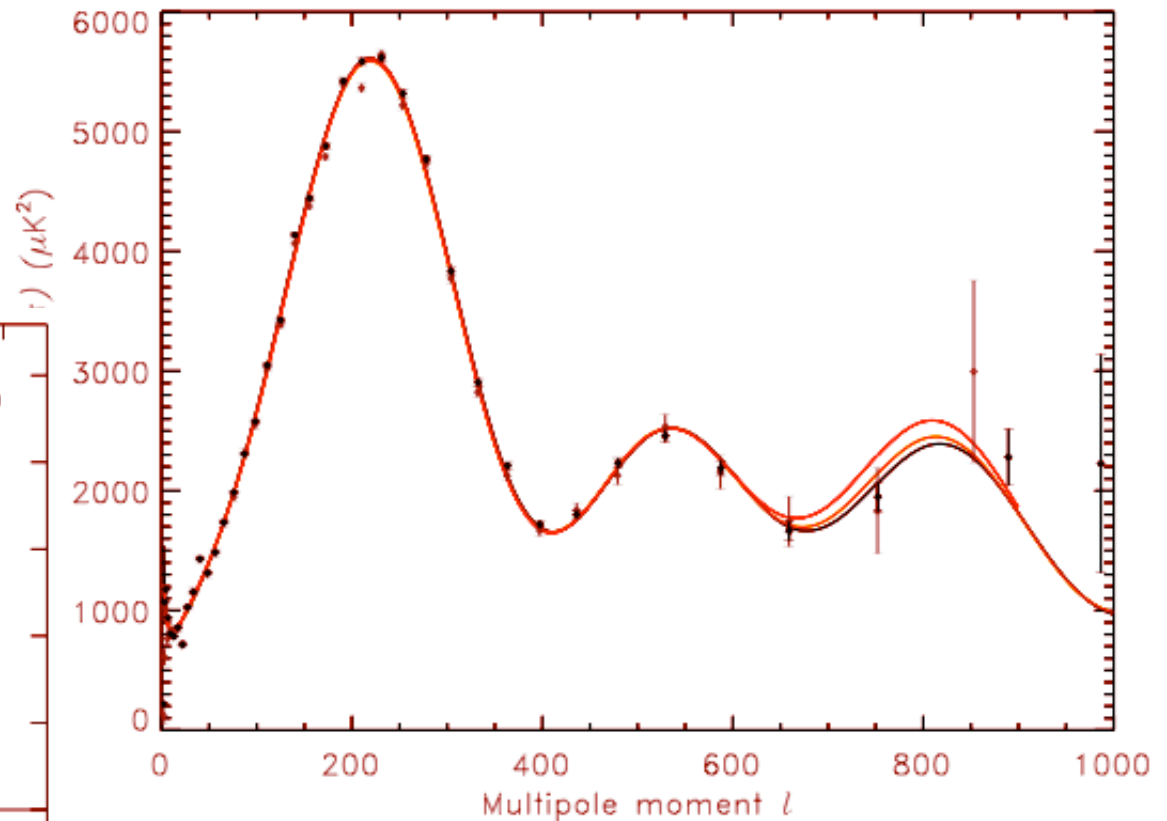
(Freedman et al. 2001,
ApJ 553, 47)

$$\Omega_K = -0.003 \pm_{0.017}^{0.013}$$

$$\Omega_\Lambda = 0.758 \pm_{0.058}^{0.035}$$



WMAP 3 year data results: *Spergel et al. 2006*



WMAP3 Constraints

Spergel et al. 2007

Power-law Λ CDM

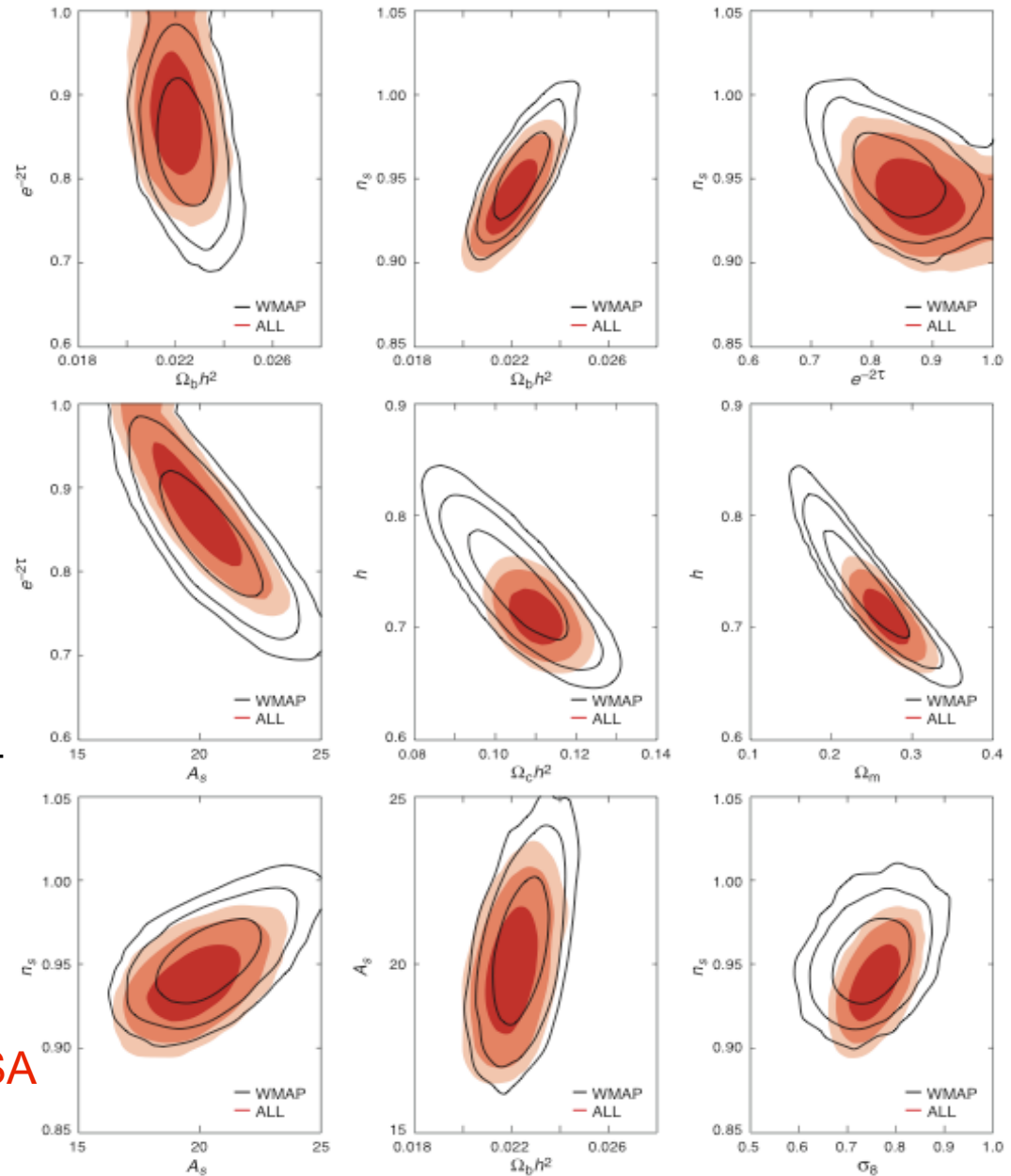
$$\Omega_M h^2 = 0.127 \pm_{0.013}^{0.007}$$

$$\Omega_B h^2 = 0.0223 \pm_{0.0009}^{0.0007}$$

$$h = 0.73 \pm_{0.03}^{0.03} \quad \text{Consistent with HST}$$

$$n_s = 0.951 \pm_{0.019}^{0.015} \quad (< 1 @ 3\sigma)$$

ALL = WMAP+2dFGRS+SDSS
+ACBAR+BOOMERanG+CBI+VSA
+SN(HST/GOODS)+SN(SNLS)



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Structures

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CMB: WMAP 3 Year Results

Assuming flat Λ CDM:

$$\Omega_B h^2 = 0.022 \pm_{0.091}^{0.072} \quad = \text{BBN}$$

$$\Omega_M h^2 = 0.1268 \pm_{0.0128}^{0.0073} \quad > \Omega_B h^2$$

With h from HST: $\Omega_M \approx 0.25$

$$\sigma_8 = 0.744 \pm_{0.060}^{0.050}$$

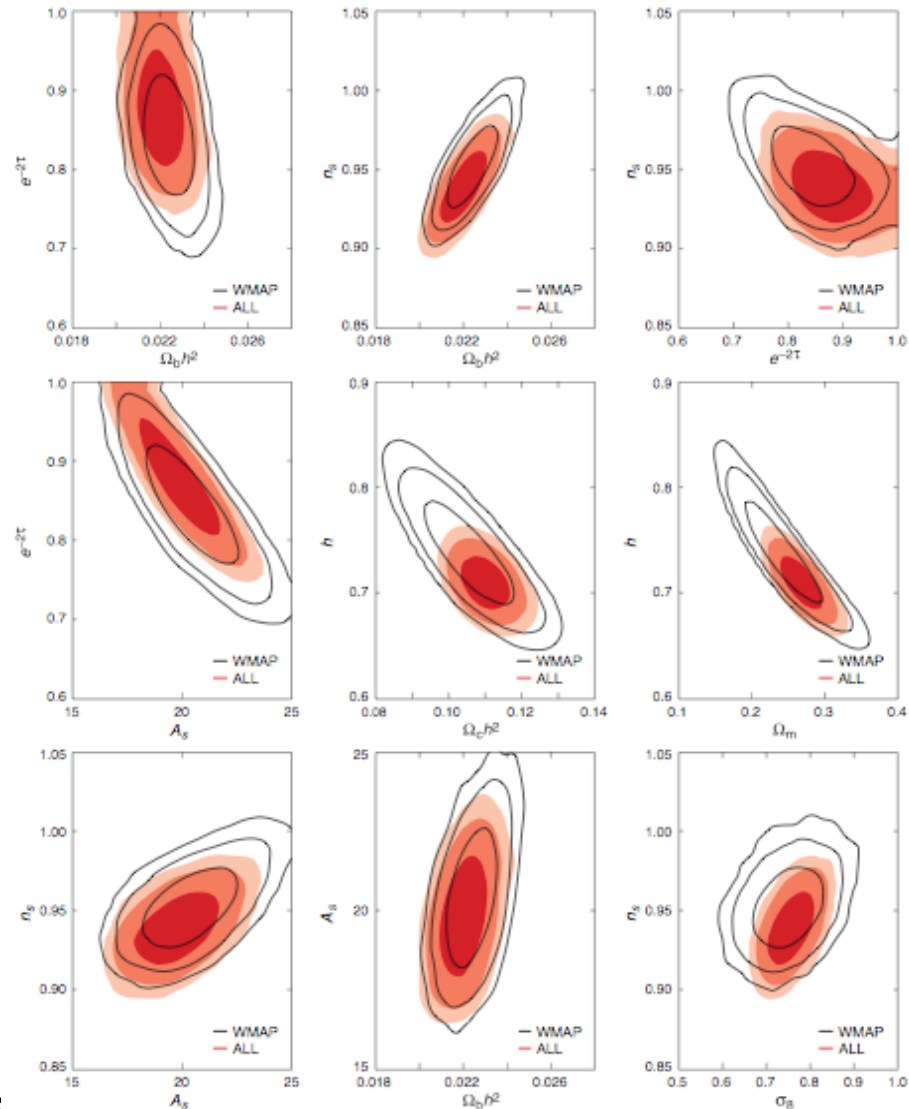
$$n_s = 0.951 \pm_{0.019}^{0.015} \quad < 1 \dots$$

$$\tau = 0.088 \pm_{0.034}^{0.028}$$

General Λ CDM + HST:

$$\Omega_K = -0.003 \pm_{0.017}^{0.013}$$

$$\Rightarrow \Omega_\Lambda \approx 0.75$$

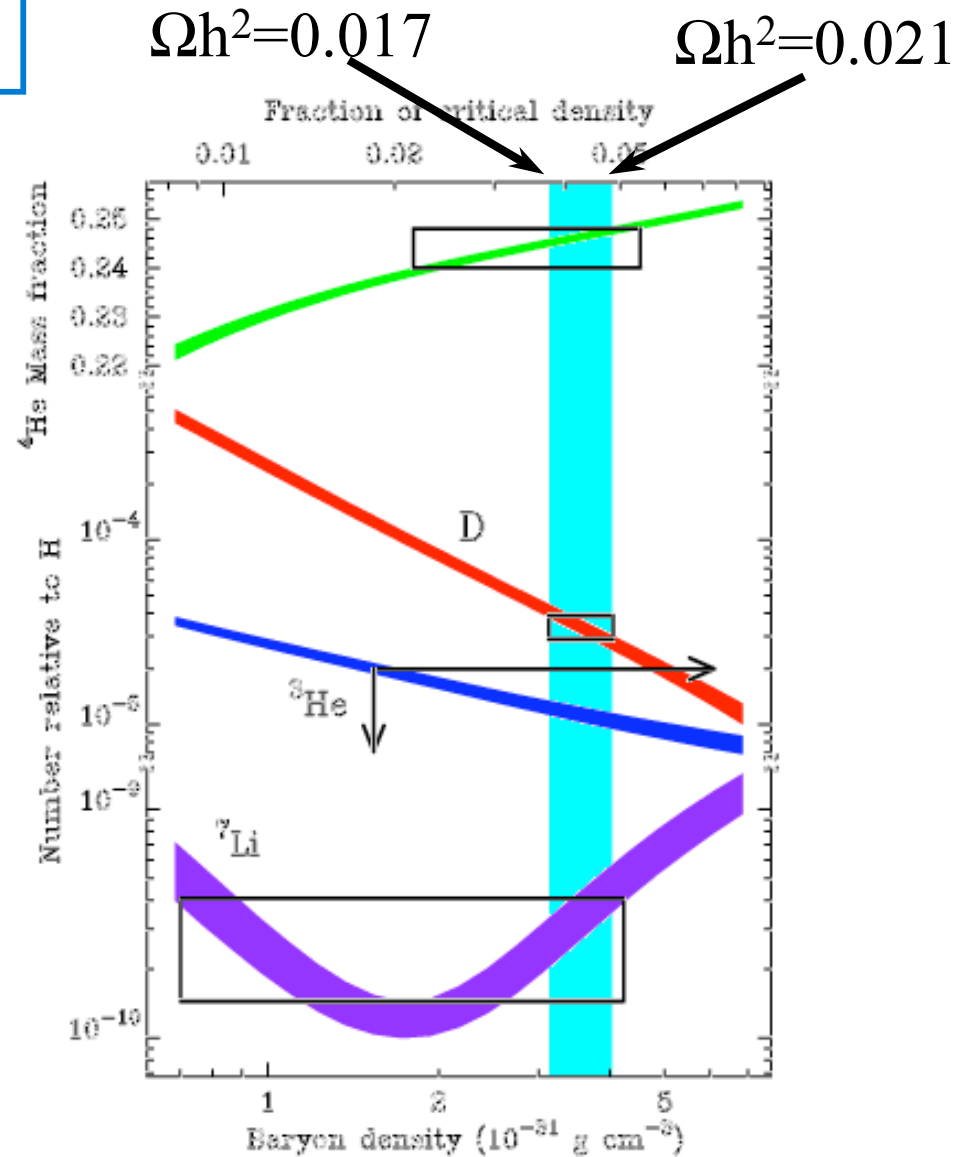
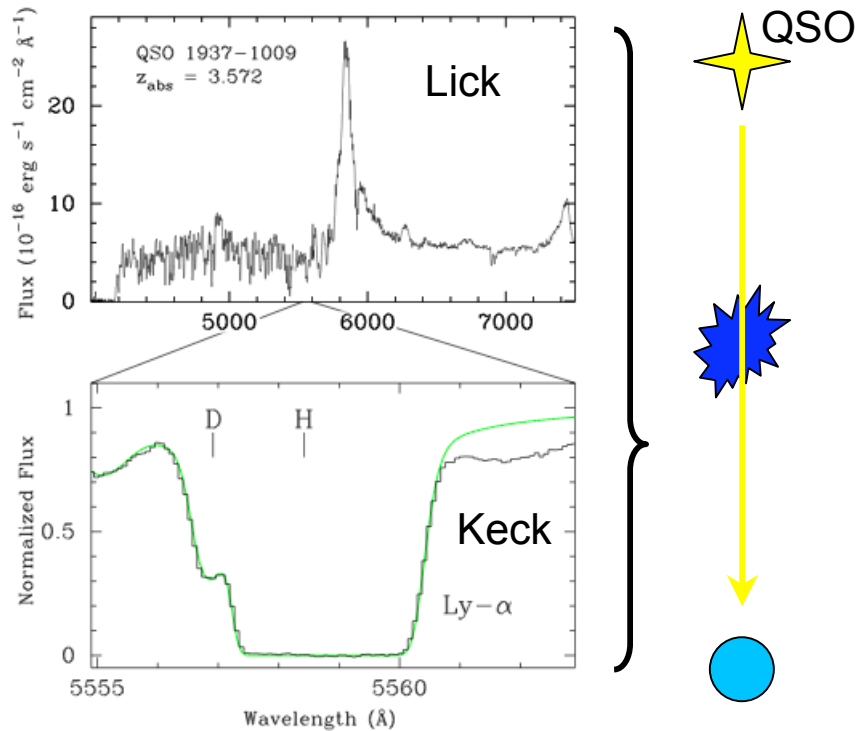


3/3/08

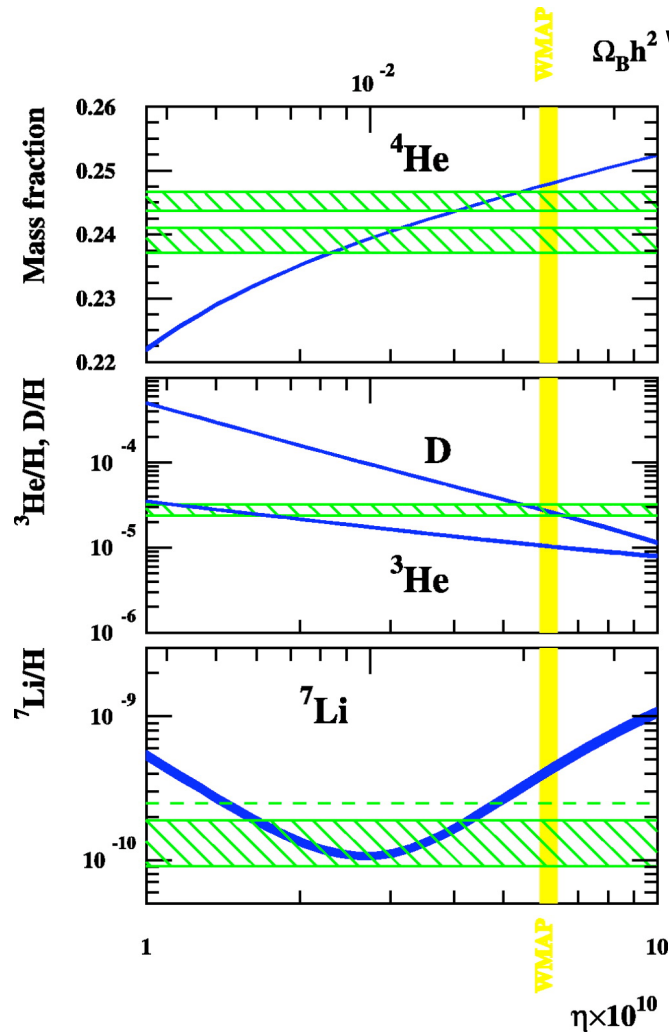
S

Tytler et al. 2001, astro-ph/0001318
(physical scripta T85, 12)

Primordial D measured in
Intergalactic clouds (Ly α forest)
High resolution spectra: **Keck**



Comparison BBN/CMB: Coc et al. 2004, ApJ 600,544



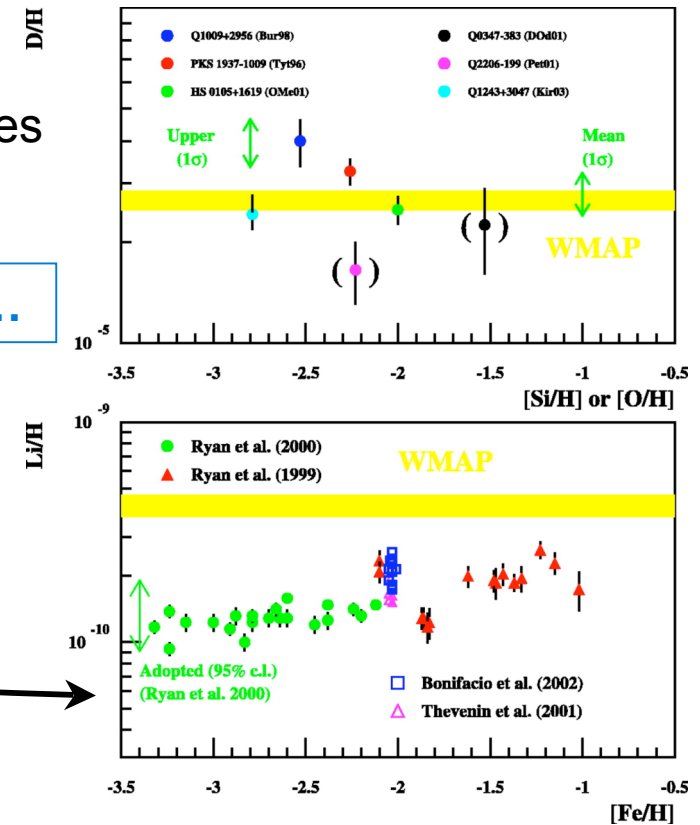
$$\Omega_B h^2 \text{ WMAP1: } \Omega_B h^2 = 0.024 \pm 0.001$$

$$(\text{WMAP3 } \Omega_B h^2 = 0.0223 \pm_{0.0009}^{0.0007})$$

Primordial $\leftrightarrow$
Measured abundances
Chemical evolution

D seems cleanest...

Li problem ?



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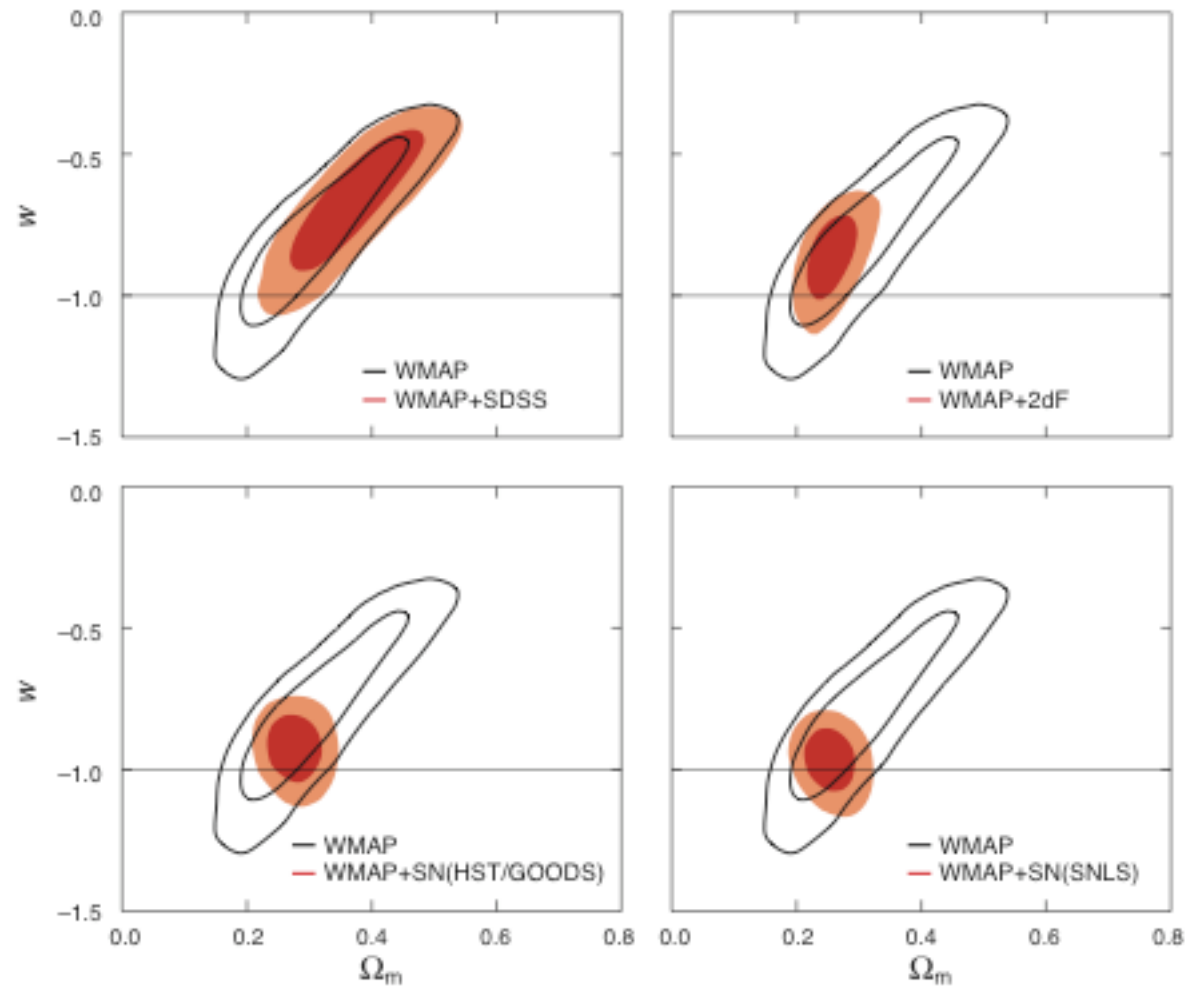
Structures

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WMAP3 Constraints: w

Spergel et al. 2007

Flat models

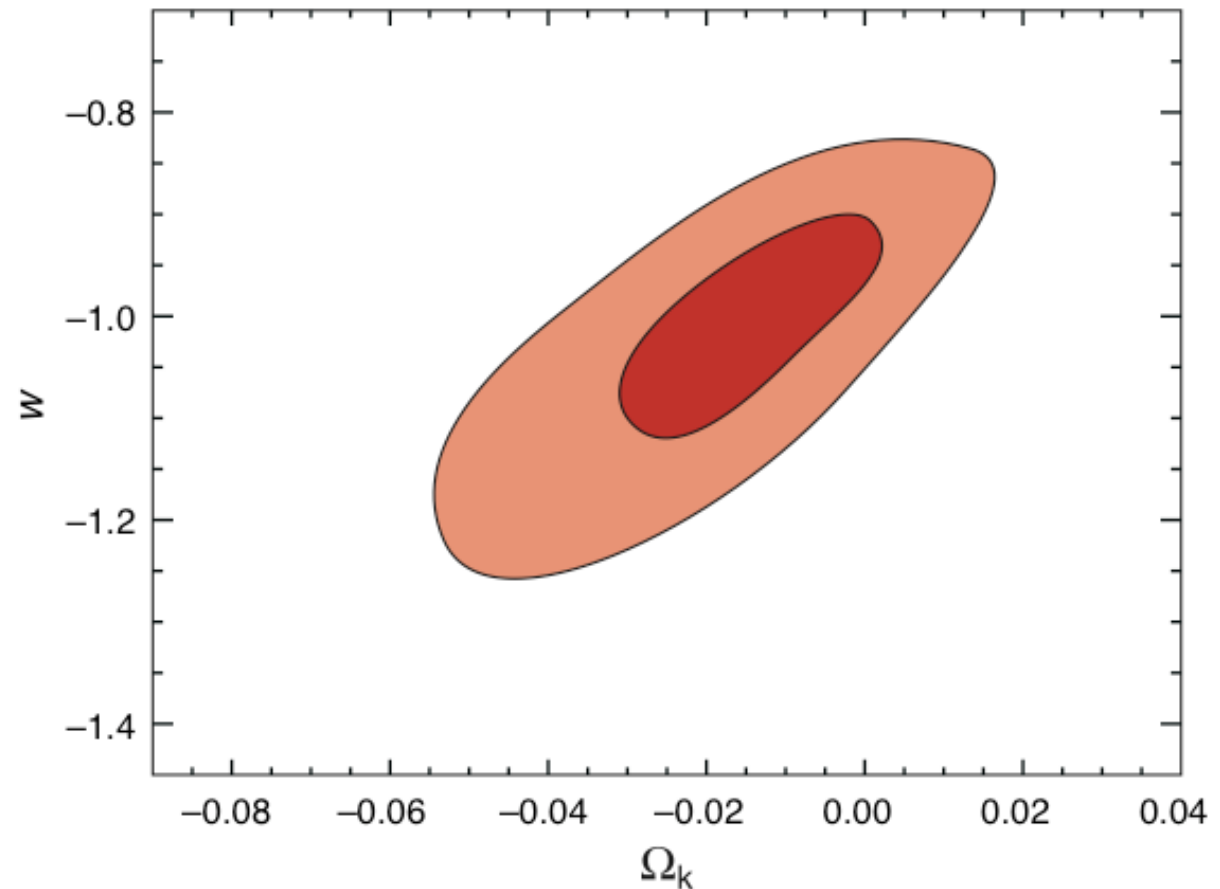


WMAP3 Constraints: w & curvature

Spergel et al. 2007

$$\Omega_K = -0.024 \pm_{0.013}^{0.016}$$

$$w = -1.062 \pm_{0.079}^{0.128}$$



WMAP3 Constraints: w & neutrino mass

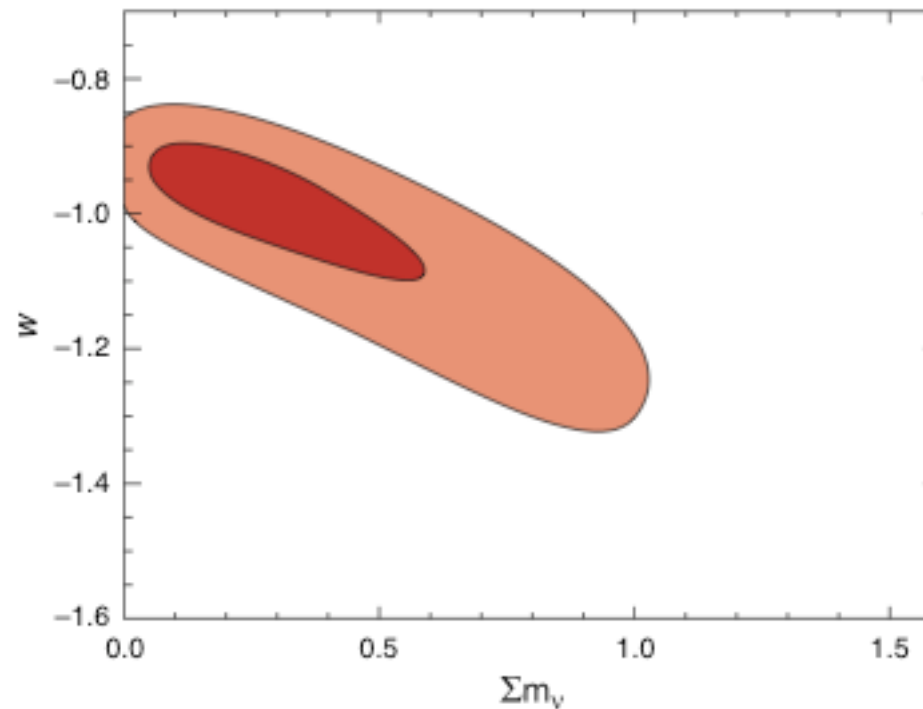
Spergel et al. 2007

Flat Models

CMB+2dFGRS
+SDSS+supernova

$$\sum m_\nu < 1 \text{ eV} \text{ (95\%)}$$

$$w = -1.06 \pm_{0.10}^{0.13}$$



Next Mission: Planck

Launch: October 31, 2008!

The Future: *Polarization*

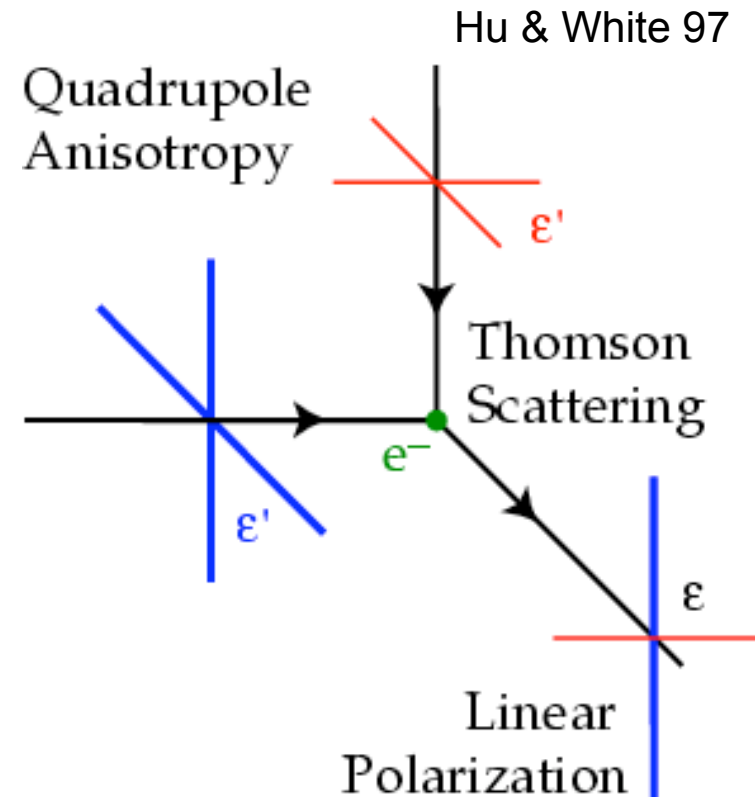
CMB Polarization Anisotropies

Thompson scattering in the plasma

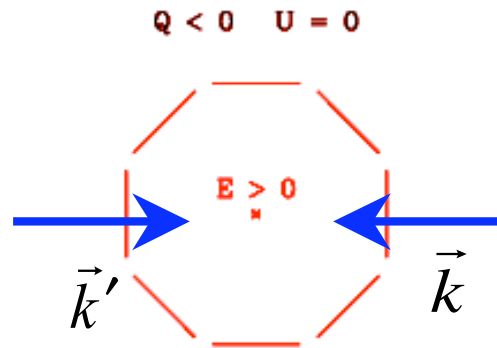
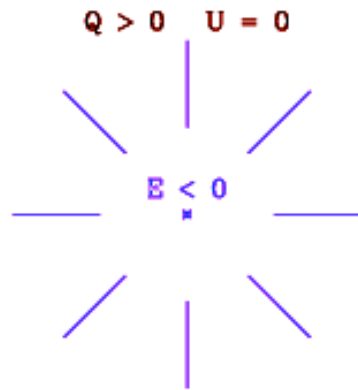
$$\frac{d\sigma}{d\Omega} = \frac{3}{8\pi} \sigma_T |\boldsymbol{\varepsilon} \cdot \boldsymbol{\varepsilon}'|^2$$

- Linear polarization
- Local quadrupole anisotropy
- Finite optical depth

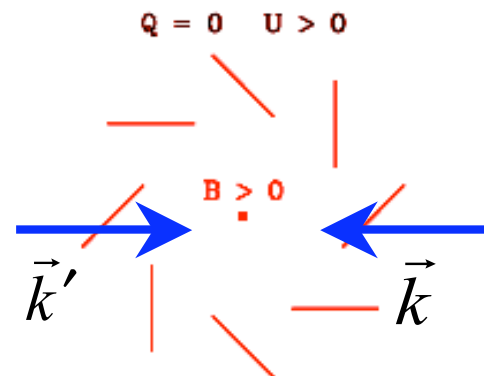
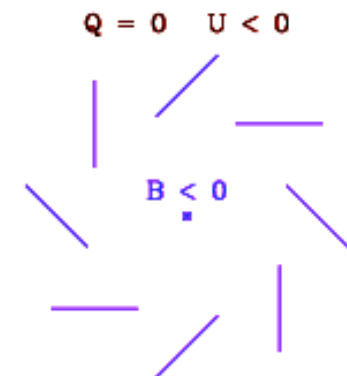
Generated by local anisotropy



Two Kinds of Spatial Patterns



E-modes (even parity)



B-modes (odd parity)

Zaldarriaga

3/3/08

Structures

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Importance of decomposition

- T (intensity), E & B can all be measured separately
- They isolate different physical processes

T spectrum

$$C_l^{TT}$$

E spectrum

$$C_l^{EE}$$

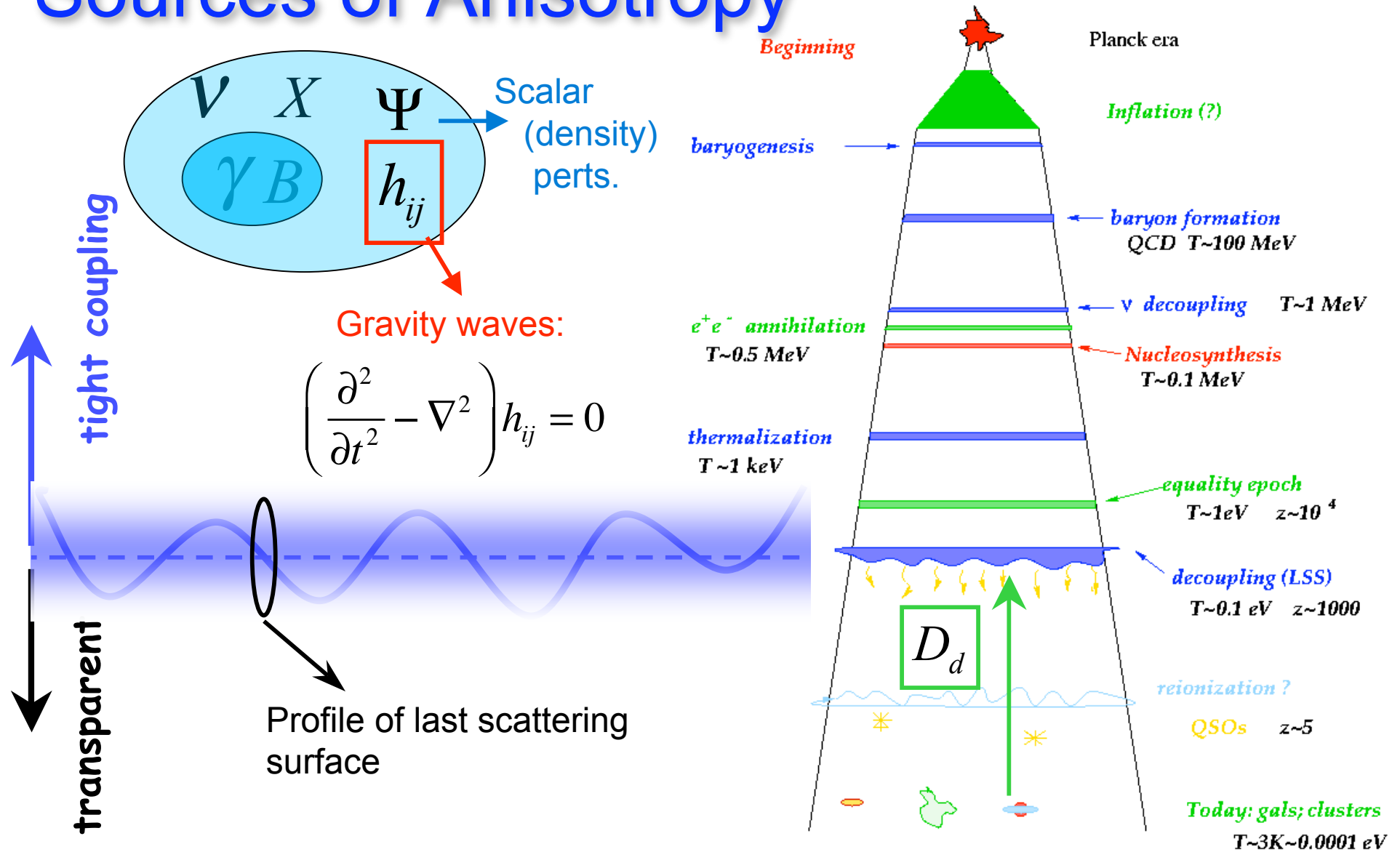
Cross TE spectrum

$$C_l^{TE}$$

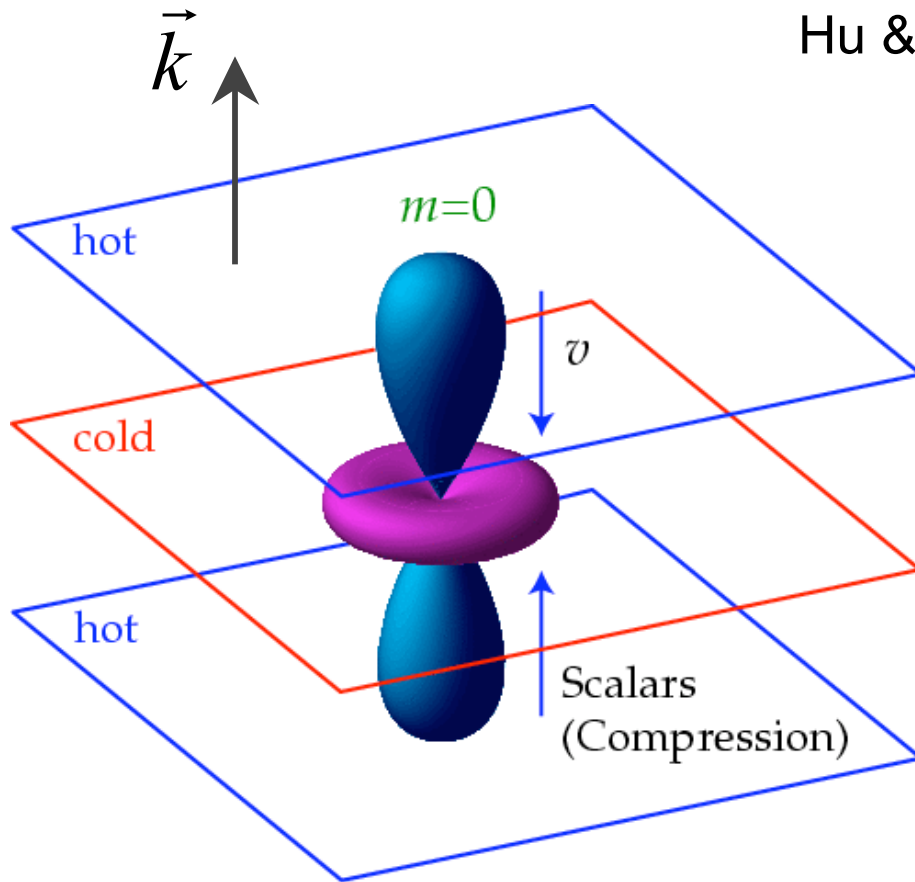
B spectrum

$$C_l^{BB}$$

Sources of Anisotropy

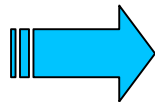


Hu & White 97

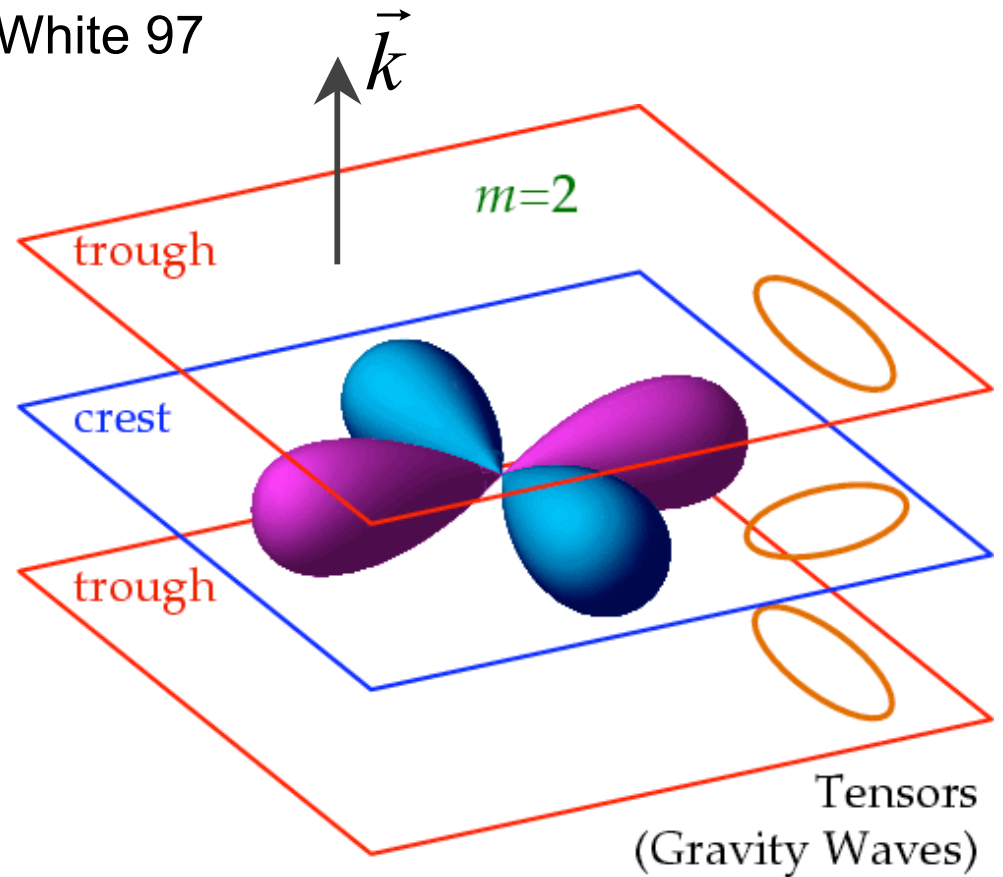


Axial symmetry around wavevector

Even parity

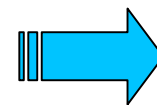


E mode



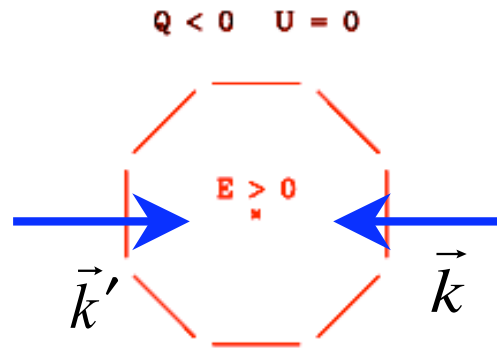
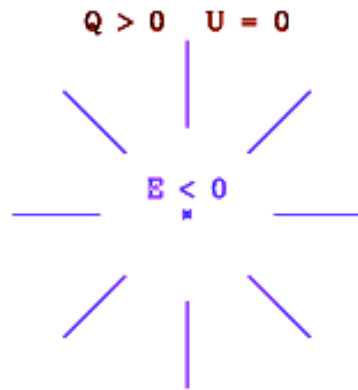
Loss of axial symmetry around wavevector

No parity



E & B modes

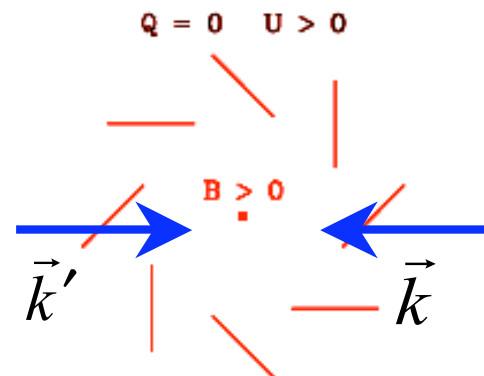
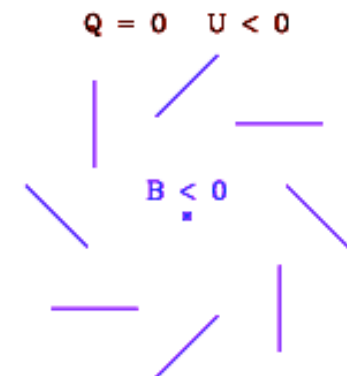
Two Kinds of Spatial Patterns



E-modes (even parity)

Density perturbations

Gravity waves



B-modes (odd parity)

Gravity waves

Gravitational lensing

Zaldarriaga

3/3/08

Structures

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Gravity Waves

Produced with CAMB

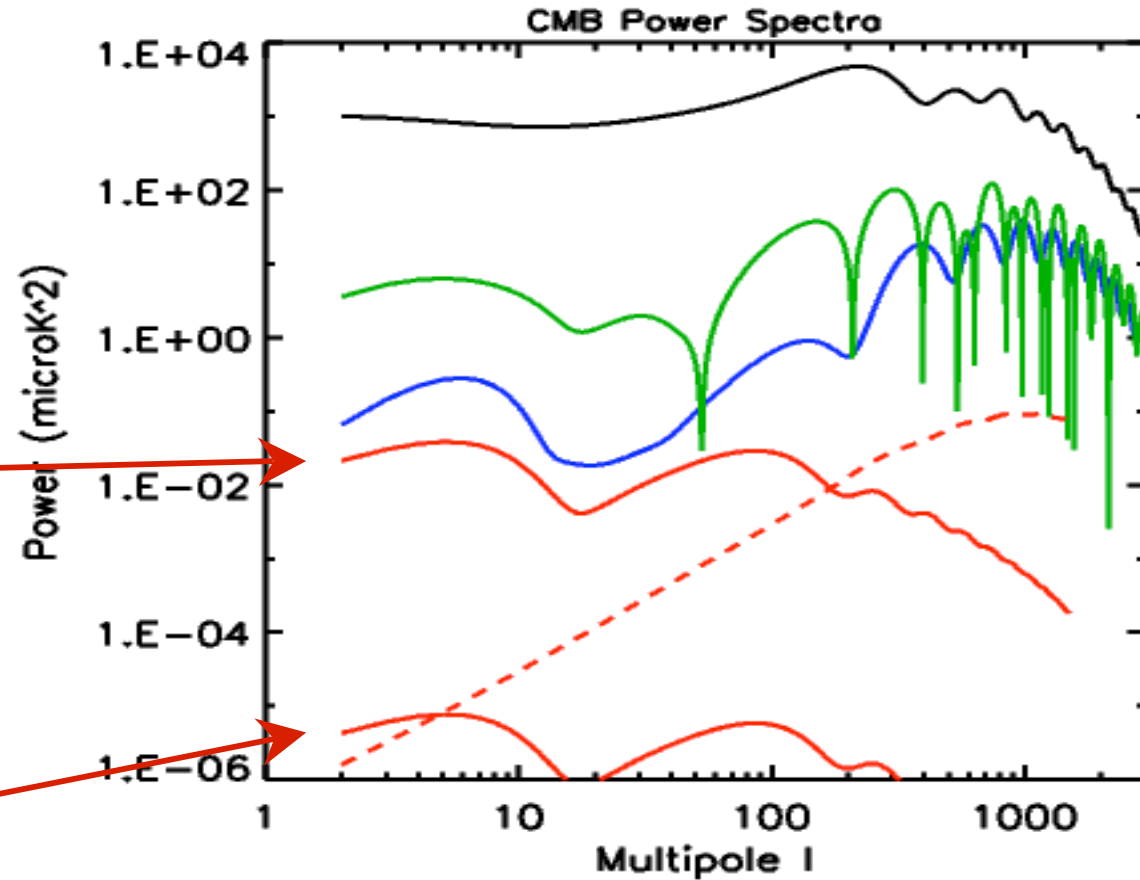
$$r \equiv \frac{T^2}{S^2} \propto \left(\frac{E_I}{M_{pl}} \right)^4$$

$$r = 0.5$$

$$E_I \sim 3 \times 10^{16} \text{ GeV}$$

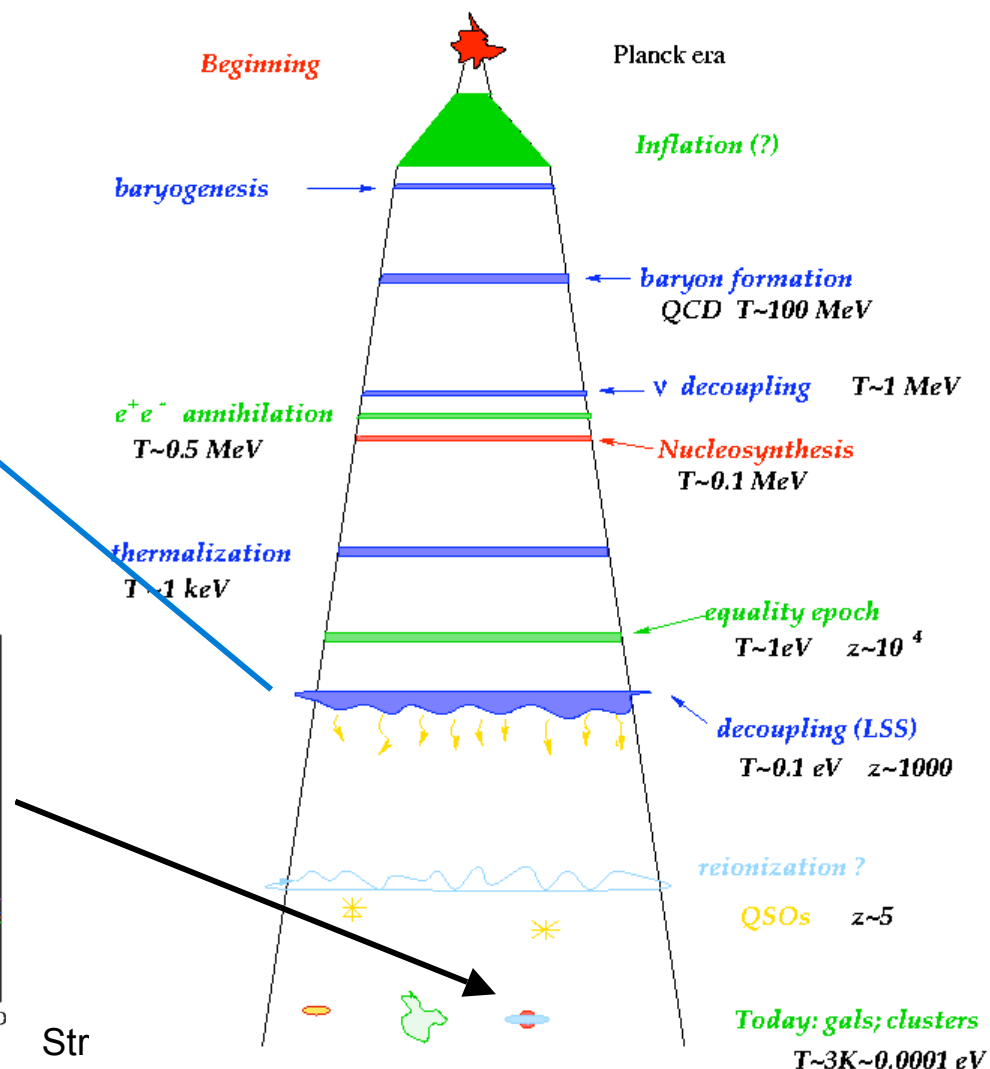
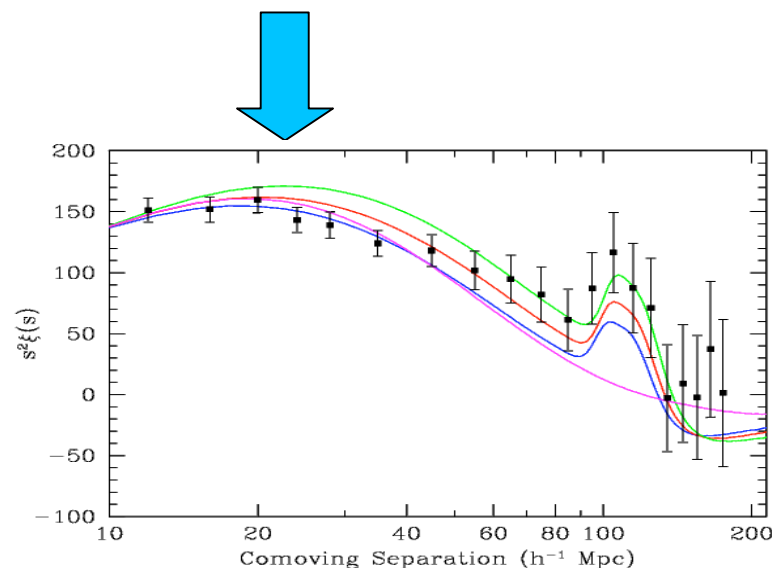
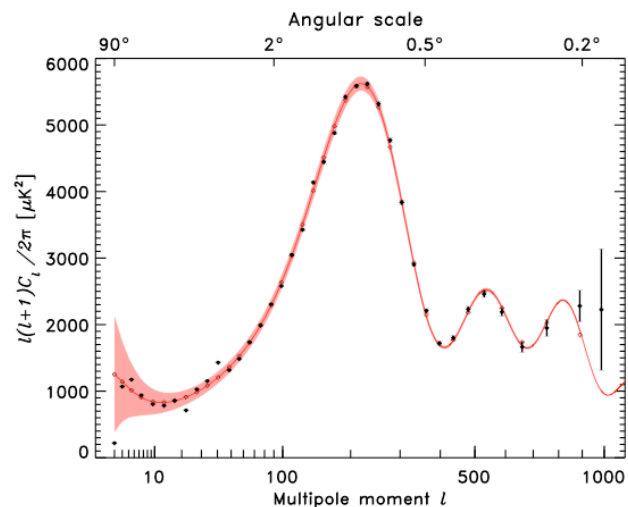
$$r = 10^{-4}$$

$$E_I \sim 3.6 \times 10^{15} \text{ GeV}$$



Fiducial WMAP-1 Model ($\tau = 0.17$)

Baryon Acoustic Oscillations



Baryon Acoustic Peak

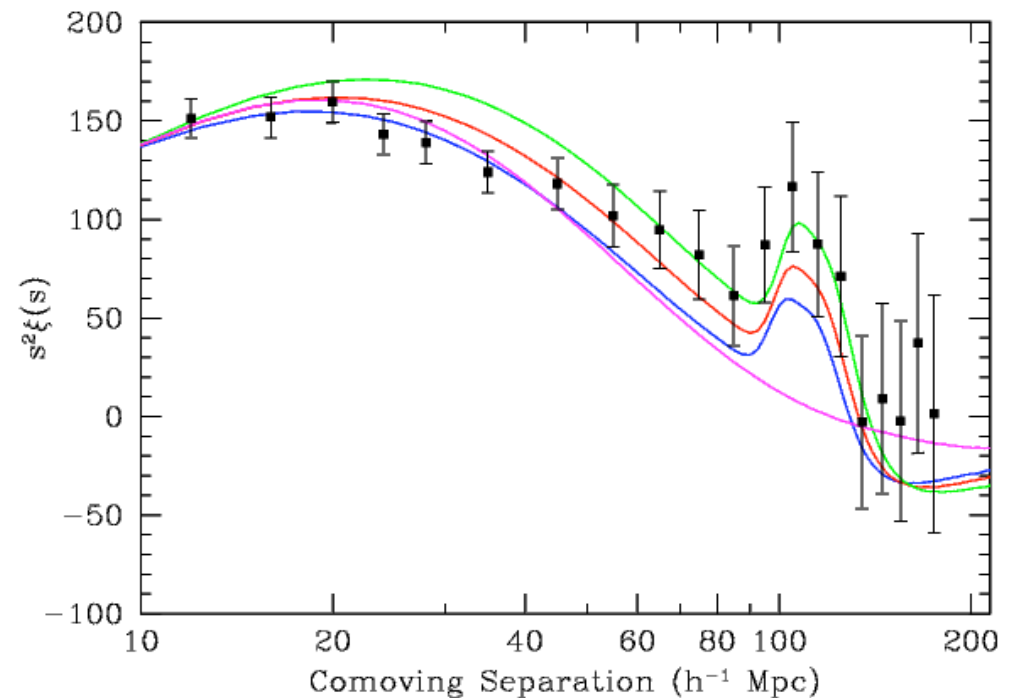
Eisenstein et al. 2005, ApJ 633, 560

- Correlation function for the Luminous Red Galaxy (LRG) sample from SDSS.

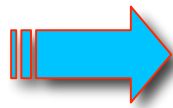
- 46,748 galaxies with $0.16 < z < 0.47$

- Peak is the same acoustic signature seen in CMB

- Effectively measures $D_{ang}(z=0.35)$



CMB (WMAP1)+SDSS



$$\Omega_R = -0.010 \pm 0.009 \quad \text{i.e., SN, HST}$$